Sodium Mobility in the NASICON Series $Na_{1+x}Zr_{2-x}In_{x}(PO_{4})_{3}$

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Rhombohedral $Na_{1+x}Zr_{2-x}In_x(PO_4)_3$ ($x=0, 0.2, 0.4, 0.8, 1.0, 1.2, 1.6,$ and 1.8) NASICON materials have been studied by XRPD, variable-temperature NPD, $31P$ and variabletemperature 23Na MAS NMR, and impedance spectroscopies. Relative 31P MAS NMR peak intensities of the five detected signals, attributed to the environments $[P(OZr)_{4-n}(OIn)_{n}]$ (*n* $(0,-4)$], are close to those expected for a random distribution of octahedral cations. This local probe allows us to rule out the existence of segregated metal-rich nanoregions. Combined NPD and XRPD Rietveld studies showed that the occupation of M2 sites by the extra Na^+ cations produces a slight distortion of the structure. Low temperatures freeze Na mobilities and permit the assignment of the resulting NMR bands to Na^+ in the M1 and M2 sites. The mobility of Na at room temperature increases with the Na content. For samples with *^x* < 0.8, Na ions are relatively localized; however, for $x \geq 0.8$, Na mobility increases, yielding a unique signal in the 23Na NMR spectra. The increase of Na mobility causes spatial disorder at the M1 site as deduced from the variable-temperature NPD study. At low temperatures, the activation energies do not change significantly. So, the observed increase in bulk conductivity by 2 orders of magnitude in the low-temperature regime is ascribed to an increase of mobile carrier, Na^+ , concentration. However, at higher temperatures a new regime has been identified by NPD, ²³Na MAS NMR, and Arrhenius plots of f_{max} data in Z'' spectra and is associated with more extended sodium motion. The onset temperature for the curvature in the Z' f_{max} Arrhenius plots, when reaching the high-temperature regime, depends on sodium content.

Introduction

NASICON materials have been extensively studied because of the high conductivity shown by some compositions.1,2 They are versatile materials and can tolerate a wide range of compositional variation. The original NASICONs were solid solutions derived from $NaZr_2P_3O_{12}$ by partial replacement of P by Si with Na excess to balance the negatively charged framework to yield the general formula $Na_{1+x}Zr_2P_{3-x}Si_xO_{12}$ ($0 \le x \le 3$). Since then, a large number of related materials have been synthesized including the series $Na_{1+x}MM(PO₄)₃$. Partial trivalent metal substitution at the octahedral metal site to give $Na_{1+x}Zr_{2-x}M_x(PO_4)_3$ has been widely studied

 $(M = Cr, Yb; ^{3}Cr, In Yb; ^{4}Al, Ga, Cr, Fe, Sc, In, Y, Yb; ^{5}$ Al, Ga, Cr, Fe, Sc, In, Y, Yb;6 In;7). The solid solution series $\text{Na}_{1+x}\text{Zr}_{2-x}\text{In}_x(\text{PO}_4)_3$ has the NASICON structure, although the compositional limit, x_{max} , has been a matter of discussion. There is one report of a complete range of solid solutions $0 \le x \le 2,5$ but other studies indicate a two-phase mixture for $x > 1.85$.^{4,7} The structure of $Na₃In₂(PO₄)₃$, recently determined from

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single-crystal data, belongs to the alluaudite type.8

The NASICON structure has a negatively charged 3D framework, of general formula $M_2X_3O_{12}$, within which the $Na⁺$ cations reside, in full or partially occupied sites. The framework is built of $XO₄$ tetrahedra linked by corners to MO_6 octahedra. Each XO_4 tetrahedron shares each corner with one MO_6 octahedron, and conversely, each MO_6 octahedron shares each corner with a different $XO₄$ group. The interstitial voids generated within the network are of two types known as M1 and M2 sites $(1:3$ multiplicity). The large counterbalance Na⁺ cations are located in these positions. An initial approach to correlate electrical parameters (ionic conductivities and activation energies) with generic average structural parameters (unit cell constants) was followed by scrutiny of specific structural factors such as the size of the bottleneck that connects the M1 and M2 sites.⁹ However, to establish possible correlations of this type, full crystal structure information is required. This may be obtained either by single-crystal diffraction or by Rietveld analysis of powder diffraction data.

Several NMR studies of NASICONs have been carried out. ³¹P MAS NMR on the $Na_{1+2x}Zr_{2-x}Mg_x(PO_4)$ ₃ series indicated a nearly random distribution of cations at the octahedral sites.¹⁰ Using ²³Na MAS NMR data for this series and the $\text{Na}_{1-x}\text{Zr}_{2-x}^{\sigma}\text{Nb}_{x}(\text{PO}_{4})_{3}$ series,¹¹ the positions of Na at M1 and M2 sites were investigated by applying inversion-recovery techniques. Using ²³Na MAS NMR data for $Na_{1+x}Zr_2(PO_4)_{3-x}(SiO_4)_x$ the quadrupolar parameters for Na at the two structural sites were estimated.¹² From variable-temperature ²³Na NMR data for $Na_{1+x}Zr_{2-x}In_x(PO_4)_3$ (not MAS), it was also possible to characterize sodium mobility.13 This series was also studied by impedance spectroscopy, although only overall conductivities were reported.7 Using a multitechnique approach, combining crystal structure determination, local structure analysis by ²³Na and ³¹P MAS NMR, and electrical conductivity measurement by impedance spectroscopy, we showed that for the phases $Na_{1.4}M_{1.6}In_{0.4}(PO_4)_3$ (M = Ti, Sn, Zr, Hf) the sizes of the bottlenecks between M1 and M2 sites correlate with ion conductivity.14

To better understand the dependence of mobility of the charge carrier with the structure and geometry of conduction pathways, the $\text{Na}_{1+x}\text{Zr}_{2-x}\text{In}_x(\text{PO}_4)$ ₃ series has been studied by different techniques: XRPD and ³¹P MAS NMR to characterize the structure combined with variable temperature neutron powder diffraction (T-NPD), 23Na T-MAS NMR and impedance spectroscopy to study the sodium mobilities.

Experimental Section

Stoichiometric amounts of Na₂CO₃, In₂O₃, (NH₄)₂HPO₄, and $ZrO₂$ (prepared as described earlier¹⁴) were heated to give the following overall reaction:

$$
{}^{(1+x)}\ell_2Na_2CO_3 + (2-x)ZrO_2 + \frac{x}{2}In_2O_3 +
$$

3(NH₄)₂HPO₄ $\xrightarrow{\Delta} Na_{1+x}Zr_{2-x}In_x(PO_4)_3 + \frac{(1+x)}{2}CO_2 +$
6NH₃ + ${}^{9}\ell_2H_2O$

The starting mixtures were ground in an agate mortar with ethanol for 1 h, dried, heated in a Pt crucible at 0.5 °C·min⁻¹ to 400 °C and left at that temperature for 1 day to release gases (NH₃, H₂O, and CO₂). To avoid unreacted $\rm ZrO_2$ and the formation of MP_2O_7 byproduct, the samples were heated at 0.5 $^{\circ}{\rm C}\cdot{\rm min^{-1}}$ to 1000 $^{\circ}{\rm C}$ with intermediate regrinding (for 30 min every 150 °C). The calcined materials were then reground in a planetary ball mill for 10 min and calcined at 1100 °C for 24 h. This last treatment was repeated twice (for all samples) to obtain homogeneous products. Nine $Na_{1+x}Zr_{2-x}In_x(\overline{P}O_4)_3$ samples were prepared for $x = 0, 0.2, 0.4, 0.8, 1.0, 1.2, 1.6$, 1.8, and 2.0 and are labeled In*x*.

XRPD patterns were collected at room temperature using a Siemens D5000 diffractometer with (*θ*/2*θ*) Bragg-Brentano geometry. To check the progress of the reaction, patterns were recorded between 13° and 50° (2*θ*) with 0.04° step size and 1 s counting time. To refine the crystal structures by the Rietveld method,15 the profiles were collected between 13° and 125° (2*θ*) with 0.03° step size and 16 s counting time.

NPD patterns for $In_{0.8}$ and $In_{1.6}$ were collected on a D1B diffractometer (at ILL) operating under standard conditions with $\lambda = 2.54$ Å at 150, 200, 250, and 275 K using a cryostat and 293, 400, and 500 K using a furnace. The bank detector (0.05° step size) was fixed to record a limited but representative region 31°-111° (2*θ*) for 10 min.

31P and 23Na MAS NMR spectra were obtained at room temperature in a MSL 400 Bruker spectrometer at 161.96 and 105.84 MHz. Samples were spun at 10-12 kHz and spectra taken after *^π*/2 pulse irradiation (3-⁴ *^µ*s). A time interval of ²-90 s between successive scans was chosen, depending on the spin-lattice relaxation times of the nuclei. The number of scans was in the range 10-30. Chemical shifts are given relative to 85% aqueous H_3PO_4 and to 1 M aqueous NaCl. To reduce Na mobility, 23Na MAS NMR spectra were also collected at ∼200 K under the same conditions. Analysis of both types of spectra was carried out using the Bruker program WINFIT. Deconvolution used a standard, nonlinear least-squares fitting method. The spinning rate and the position, line width, and intensity of components are determined automatically. However, chemical shift anisotropies (∆*σ* and *η*) for 31P and quadrupole constants (*ν*^Q and *η*) for 23Na are adjustable parameters that must be determined by trial and error.

Impedance data were collected on cylindrical pellets (∼10 mm diameter and $\sim\!1$ mm thickness) obtained by pressing fine powder at 150 MPa, for 30 s, with 3 wt %/vol PVA aqueous solution added as a binder (one drop each \sim 0.2 g). The pellets were heated at 2 °C/min to 800 °C to remove organic matter, sintered at 1230-1300 °C for 2 h, and quenched to room temperature. To reduce possible volatilization of soda, pellets were covered with powder of the same sample during sintering. The porosities estimated from the pellet mass and geometry were in the range $8-23%$ (sample with $x = 0$ was impossible to sinter). Electrodes were made by coating opposite pellet faces with In-Ga alloy (∼1:1). The impedance data were collected using a Hewlett-Packard 4192A impedance analyzer over the frequency range from 5 Hz to 13 MHz. The samples were studied from -25 to 200 °C at approximately 15 °C intervals. The pellets were mounted in a conductivity jig whose leads were shielded separately inside a tube furnace or a Dewar. For low-temperature measurements, the samples were allowed to equilibrate for ∼1 h prior to measurements; temperatures were accurate to ± 1 °C.

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Table 1. Some Crystallographic Parameters and Activation Energies for the Na1+*^x***Zr2**-*^x***In***x***(PO4)3 Series***^a*

sample	$R_{\rm WP}/\%$	$R_{\rm P}/\%$	$R_{\rm F}/\%$	$a/\text{\AA}$	$c/\text{\AA}$	V/\AA ³	ρ /g cm ⁻³	area $T1/\AA^2$	area $T2/\AA^2$	$E_a(f_{\text{max}} M')/eV$
In_0	9.70	7.13	3.34	8.80655(5)	22.7541(2)	1528.28(2)	3.197	5.21(4)	5.47(3)	
$In_{0.2}$	10.38	7.55	3.02	8.81983(9)	22.7217(3)	1530.71(3)	3.252	5.20(4)	5.54(4)	0.49
$In_{0.4}$	10.98	8.10	3.51	8.83778(11)	22.6913(4)	1534.89(4)	3.304	5.20(5)	5.52(4)	0.45
$In_{0.8}$	11.43	8.66	4.39	8.86977(8)	22.5912(3)	1539.21(3)	3.415	5.21(5)	5.56(4)	0.42
	2.89	2.03	3.01							
$In_{1,0}$	11.58	9.06	4.84	8.88637(7)	22.5432(2)	1541.68(3)	3.470	5.24(5)	5.61(4)	0.39
In _{1.2}	12.01	9.21	5.58	8.90246(6)	22.4943(2)	1543.92(2)	3.525	5.18(6)	5.48(5)	0.42
In _{1.6}	13.01	9.58	4.34	8.93731(10)	22.4044(4)	1549.81(4)	3.631	5.19(6)	5.66(6)	0.46
	2.38	1.69	3.75							
In _{1.8}	11.63	8.64	4.21	8.95549(7)	22.3539(3)	1552.61(3)	3.685	5.20(5)	5.53(5)	0.43

^a NPD R-factors are given in italics.

Results

Rietveld Study. Initial XRPD data indicated that the members of this series for $x < 1.8$ are crystalline single phases which have the rhombohedral *R*3c NA-SICON-type structure. The $x = 2$ sample, $Na₃In₂(PO₄)₃$, was a mixture of a NASICON-type phase plus an alluaudite type phase and was not studied further. The crystal structures were refined by the Rietveld method using the structure of $NaZr_2(PO_4)_3$ as starting model.¹ The nominal Zr/In contents were assumed to be randomly distributed over the octahedral sites. It was also assumed, in the starting model, that there was full occupancy of the Na(1) site at (0 0 0; 6b Wyckoff notation) and random distribution of the sodium excess on the M2 site $(0.65 \ 0.1/4; 18e)$. Then, the common overall parameters, scale factor, background coefficients, unit cell parameters, zero-shift error, and pseudo-Voigt coefficients,¹⁶ corrected for asymmetry,¹⁷ were optimized.

It became apparent, during an early stage of the refinements, that experimental peak intensities, especially those for $In_{1.6}$ and $In_{1.8}$, were not reproducible. This was due to the presence of large microparticle aggregates (grains) without random orientation. This "preferred orientation" could not be taken into account using the March-Dollase correction.¹⁸ Instead, the successfully adopted method was to prepare random samples using the TASC (*t*ubular *a*erosol *s*uspension *chamber*) method¹⁹ in which aerosol particles of NASI-CON were generated by convection in a fluidized bed of glass beads mixed with the NASICON powder. This method of preparation, for $In_{1.6}$ and $In_{1.8}$, gave a highly uniform layer of small particles randomly distributed on a glass fiber filter substrate with reproducible XRPD peak intensities.

Once instrumental parameters had been taken into account, positional parameters were refined with the Zr/In ratios fixed at their expected values. This assumption was supported by the absence of impurity phases and by the quantitative analysis of the $31P$ MAS NMR spectra (see below). The XRPD refinements of the initial model, with full occupancy of Na(1) and the excess sodium on the Na(2) site, yielded large isotropic tem-

perature factors for Na(1), $U_{\text{iso}} \approx 0.10 \text{ Å}^2$, for samples with high *x*. These anomalously large values may be due to either spatial disorder or an occupancy lower than 1.00. Combined room temperature XRPD and NPD refinements for $In_{1.6}$ and $In_{1.8}$ showed that spatial disorder inside the M1 cavity was the main cause of the high temperature factors. Within two times the standard deviation, 1.5%, full occupancy of the M1 site was obtained in these two combined room temperature refinements. Finally, an isotropic temperature factor for each crystallographic framework site was refined. Rietveld analyses of the T-NPD data indicate the temperature at which positional disorder appears. Due to the limited 2*θ* range, only isotropic temperature factors were refined and positional parameters and occupation factors were kept fixed at the values obtained in the room temperature combined refinements. The *U*iso values obtained for Na at the M1 site (000) are anomalously very high, [∼]0.15 Å2 at *^T* ^g 400 K.

Final Rietveld figures of merit were good (Table 1) with R_F ranging between 3 and 6%. Final refined unit cell parameters are also given in Table 1, atomic parameters in Table 2, selected distances in Table 3, and angles in Table 4. The areas of the bottleneck triangles, as defined in ref 14, are given in Table 1. As an example of the Rietveld refinement quality, the fit for the combined refinement of $In_{1.6}$ is shown in Figures 1 and 2. The isotropic temperature factors for sodium atoms obtained from the T-NPD analyses are plotted in Figure 3.

MAS NMR Study. Room temperature 31P MAS NMR spectra for the $Na_{1+x}Zr_{2-x}In_x(PO_4)_3$ series (Figure 4) are formed by five components with their corresponding spinning sidebands (not shown). In the NASICON structure, each tetrahedron shares oxygens with four octahedra, two in the same $M_2(PO_4)_3$ unit and two in adjacent units. On the basis of homogeneous statistical distribution of tri- and tetravalent cations, the five observed components can be assigned to $P(OZr)_{4}$, $P(OZr)_{3}$ - $(OIn)_1$, $P(OZr)_2(OIn)_2$, $P(OZr)(OIn)_3$, and $P(OIn)_4$ environments. The position of the 31P MAS NMR peaks depends on the polarizing strength of cations that share oxygens with the $PO₄$ tetrahedra. Thus, strongly polarizing cations pull the electron density away from oxygens more effectively and cause the NMR peaks to shift to more negative values. This effect is cumulative and produces the five components detected in 31P MAS NMR spectra (Figure 4 and Table 5). The peaks occur at increasingly negative chemical shifts as the number of Zr neighbors increases. In addition to this "first-order" effect, in which the chemical shift values depend on the

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Table 2. Refined Structural Parameters for the Na1+*^x***Zr2**-*^x***In***x***(PO4)3 Series**

		In_0	$In_{0.2}$	$In_{0.4}$	$In_{0.8}$	$In_{1.0}$	In _{1.2}	In _{1.6}	In _{1.8}
$Na(1)$ (6b)	$U_{\rm iso} \times 100$	3.4(2)	4.0(2)	4.7(3)	$0.9(5)$ ^a	10.1(5)	10.2(5)	$3.1(9)^{b}$	12.5(6)
(0 0 0) $Na(2)$ (18e)	\boldsymbol{X}		0.618(8)	0.621(5)	0.636(2)	0.632(2)	0.634(2)	0.639(1)	0.637(1)
(X 0 ¹ /4)	$U_{\rm iso}\times 100$		$3(-)$	6(2)	4.3(6)	2.9(5)	5.1(5)	3.6(3)	2.2(3)
$Zr-In(12c)$	Z	0.14561(4)	0.14596(5)	0.14659(5)	0.14760(5)	0.14800(5)	0.14850(5)	0.14896(6)	0.14961(4)
(00z)	$U_{\rm iso}\times 100$	0.43(3)	0.40(3)	0.42(4)	0.65(4)	0.66(3)	0.77(3)	0.50(4)	0.44(3)
P(18e)	\boldsymbol{X}	0.2919(3)	0.2938(3)	0.2947(4)	0.2960(3)	0.2957(4)	0.2951(4)	0.2942(3)	0.2971(4)
(X 0 ¹ / ₄)	$U_{\rm iso}\times 100$	0.84(7)	0.74(9)	0.75(10)	1.22(9)	0.92(9)	0.92(10)	0.99(11)	0.82(9)
$O(1)$ (36f)	\boldsymbol{X}	0.1854(5)	0.1869(6)	0.1881(7)	0.1869(3)	0.1900(7)	0.1870(7)	0.1913(4)	0.1930(7)
(x y z)	У	$-0.0191(6)$	$-0.0222(7)$	$-0.0229(8)$	$-0.0212(3)$	$-0.0272(8)$	$-0.0292(8)$	$-0.0234(4)$	$-0.0227(8)$
	Z	0.1965(2)	0.1958(2)	0.1960(3)	0.1958(1)	0.1956(3)	0.1960(3)	0.1949(1)	0.1943(3)
	$U_{\rm iso}\times 100$	1.2(1)	1.3(2)	1.5(2)	2.1(1)	1.9(2)	2.7(2)	2.8(1)	2.8(2)
$O(2)$ (36f)	\boldsymbol{X}	0.1912(5)	0.1916(5)	0.1913(5)	0.1907(3)	0.1954(5)	0.1929(6)	0.1895(3)	0.1908(6)
(x y z)	У	0.1672(5)	0.1697(5)	0.1694(6)	0.1710(3)	0.1728(6)	0.1692(6)	0.1727(3)	0.1724(6)
	Z	0.0856(2)	0.0860(2)	0.0854(2)	0.0871(1)	0.0866(2)	0.0850(3)	0.0870(1)	0.0871(2)
	$U_{\rm iso}\times 100$	1.0(1)	0.5(1)	0.5(2)	0.6(1)	0.6(1)	1.1(2)	0.3(1)	0.7(2)

a Joint NPD and XRPD. Na1 at (0.056(24), 0.051(42), 0.001(5)). *b* Na1 at (0.066(34), 0.054(35), 0.001(6)), occ. factor = 0.167.

Table 3. Selected Distances (Å) for the Na1+*^x***Zr2**-*^x***In***x***(PO4)3 Series**

	In_0	$In_{0.2}$	$In_{0.4}$	$In_{0.8}$	$In_{1,0}$	In _{1.2}	$In_{1.6}$	$In_{1.8}$	% relative increase ^a
$M-O(1) \times 3$	2.075(4)	2.088(4)	2.098(5)	2.069(2)	2.114(5)	2.101(6)	2.094(3)	2.093(6)	$+0.9$
$M-O(2) \times 3$	2.094(4)	2.103(4)	2.120(5)	2.113(2)	2.150(5)	2.161(5)	2.137(2)	2.150(6)	$+2.7$
$P-O(1) \times 2$	1.495(4)	1.503(5)	1.496(6)	1.512(2)	1.489(6)	1.490(6)	1.490(3)	1.507(7)	$+0.8$
$P-O(2) \times 2$	1.547(4)	1.528(4)	1.529(4)	1.527(2)	1.500(4)	1.530(5)	1.547(3)	1.530(5)	-1.1
$Na(1)-O(2) \times 6$	2.514(4)	2.527(4)	2.515(5)	b.	2.553(5)	2.507(5)	b.	2.540(5)	$+1.0$
$Na(2)-O(1) \times 2$	3.05 ^c	3.01(5)	2.99(4)	2.90(1)	2.90(1)	2.87(1)	2.898(7)	2.923(9)	-4.2
$Na(2)-O(1) \times 2$	2.77c	2.744(9)	2.745(8)	2.758(4)	2.721(6)	2.735(7)	2.708(3)	2.684(6)	-3.1
$Na(2)-O(2) \times 2$	2.33c	2.35(6)	2.38(4)	2.479(14)	2.472(14)	2.502(14)	2.496(8)	2.502(9)	$+7.4$
$Na(2)-O(2) \times 2$	2.43c	2.442(15)	2.440(10)	2.443(3)	2.437(6)	2.424(6)	2.480(3)	2.476(5)	$+1.9$
$Na(1)\cdots Na(2) \times 6$	3.327(1)	3.340(21)	3.352(15)	_b	3.388(6)	3.398(6)	b	3.416(3)	$+2.3$
$Na(2)\cdots Na(2) \times 4$	4.734(1)	4.76(4)	4.794(31)	4.904(12)	4.884(12)	4.908(12)	4.959(7)	4.959(7)	$+2.7$
$Na(2)\cdots Na(2) \times 4$	4.675(1)	4.681(15)	4.687(11)	4.711(4)	4.697(4)	4.700(4)	4.705(2)	4.699(2)	$+0.5$
$M \cdots M^d$	4.751(2)	4.728(2)	4.693(2)	4.627(2)	4.599(2)	4.566(2)	4.528(2)	4.488(2)	-5.5
$\mathbf{M}\cdots\mathbf{M}^e$	6.626(2)	6.633(2)	6.653(2)	6.669(2)	6.673(2)	6.681(2)	6.675(2)	6.688(2)	$+0.9$

a Relative increase = $100 \times (X_{1.8} - X_0)/X_0$. *b* Several distances due to spatial disorder. *c* Calculated distances for an imaginary atom at α 61.0 ¹/a position *d* Intralantern distance (along caxis) *c* Interla the (0.61 0 1/4) position. *^d* Intralantern distance (along *c*-axis). *^e* Interlantern distance (along *c*-axis).

number of Zr neighbors, there is a more subtle "second order" effect in which the *δ* values for a given peak become more positive with increasing In content (as shown by the slightly tilted dotted lines in Figure 4).

From the integrated intensities of the five observed 31P MAS NMR bands, the chemical composition of samples can be determined. In particular, Zr/In ratios can be calculated from the expression:

$$
Zr/\text{In} = \frac{4I_0 + 3I_1 + 2I_2 + I_3}{1I_1 + 2I_2 + 3I_3 + 4I_4} \tag{1}
$$

where intensities I_i , with $i = 0, 1, 2, 3$ and 4, correspond to components with an increasing number of In atoms. From Zr/In ratios, the Zr $(2 - x)$ and In (x) contents of octahedra can be deduced, using the expression:

$$
Zr/\text{In} = (2 - x)/x \tag{2}
$$

The deduced occupancies (Table 6) are very close to the nominal values used in the sample preparation.

23Na MAS NMR spectra are given in Figure 5. The spectrum for $NaZr_2(PO_4)_3$ is formed by three sharp peaks at -18 , -32 , and -42 ppm that correspond to a unique signal produced by second-order quadrupole effects, related to the interaction of Na with the electric field gradient at sites with axial symmetry $v_Q \sim 1.2 \text{ MHz}$ and $\eta = 0$). The isotropic chemical shift value corrected for quadrupole effects was -14 ppm and line-broadening deduced from the spectral deconvolution was $E_m = 0.9$ ppm. Spectra for $In_{0.2}$ and $In_{0.4}$ are formed by a similar set of peaks, but the intensity of the peak at -32 ppm and the line width of the components increase with *x*. The experimental profile could not be reproduced with a single signal, indicating that there are at least two components. Two signals centered at ca. -13 and -17 ppm with similar quadrupole constant ($v_Q \sim 1.1$ MHz)

Figure 1. Room temperature XRPD Rietveld plot for Na_{2.6}- $Zr_{0.4}In_{1.6}(PO_4)_3.$

Figure 2. Room temperature NPD Rietveld plot for Na_{2.6}Zr_{0.4}- $In_{1.6}(PO₄)₃.$

Figure 3. Temperature evolution of the isotropic thermal parameter for Na at M1 and M2 sites of samples $In_{1.6}$ and $In_{0.8}$ from NPD data. The lines are B-spline fits only to guide the eye.

but different *η* values, 0 and 0.8, give a satisfactory fit to these spectra. The average line broadenings were 8 and 17 ppm for $In_{0.2}$ and $In_{0.4}$, respectively. For $x \ge 0.8$ phases, a single signal with axial characteristics was detected. The experimental envelope became sharper and shifted toward more positive chemical shifts as *x* increased.

 $Na_{1.0}$ \mathbf{g} -24 -32 δ (ppm) $\mathbf 0$ -8 -16

Figure 4. Centerbands of 31P MAS NMR spectra for the Na1+*^x*Zr2-*^x*In*x*(PO4)3 series.

Table 5. Chemical Shift Values of 31P MAS-NMR Components of Na1+*^x***Zr2**-*^x***In***x***(PO4)3 Samples**

sample	In_4^a	In ₃ Zr	In ₂ Zr ₂	In Z_{r_3}	Zr ₄
In_0					-24.3
$In_{0.2}$			-16.1	-20.2	-24.0
$In_{0.4}$		-11.7	-15.7	-19.7	-23.8
\ln_{0} s	-8.4	-11.5	-15.2	-19.1	-23.4
$In_{1.0}$	-8.3	-11.3	-14.9	-18.9	-23.1
\ln_{12}	-8.1	-11.2	-14.7	-18.7	-23.1
In _{1.6}	-7.9	-11.0	-14.5	-18.4	-
In _{1.8}	-7.7	-10.8	-14.6		

^a The value for the In₄ environment is calculated by linear extrapolation, assuming a constant peak separation, from positions of the other components.

Table 6. Distribution of 31P MAS-NMR Peak Intensities: Selected Intensity Ratios, Calculated Zr/In Ratio in Octahedral Sites (using eq 1) and Fractional Occupancy of Octahedral Site by in (Using Eq 2) Determined by NMR

sample					$4I_0/I_1$ $6I_1/4I_2$ $4I_2/6I_3$ $I_3/4I_4$ Zr^{4+}/In^{3+}	x , In (NMR)
\ln_{0}	6.5	10.4			9.7	0.23
$In_{0.4}$	3.4	3.9	4.5	4.0	4.0	0.42
\ln_0 s	1.1	1.5	1.6	1.7	$1.5\,$	0.82
In ₁₀	0.83	0.97	1.04	1.03	1.0	1.01
In ₁₂	0.51	0.60	0.81	0.57	0.69	1.20
In _{1.6}		0.26	0.28	0.27	0.27	1.60
In _{1.8}			0.07	0.11	0.10	1.81

Low temperature (∼200 K) 23Na MAS NMR spectra are given in Figure 6. As previously reported for $\mathop{\mathrm{In}}\nolimits_{0.4}$, 14 a new band at more positive chemical shifts appears on cooling whose relative intensity increases with *x*. Line widths of the components are larger than those measured at room temperature (Figures 5 and 6). A small shift of the experimental envelope toward low-field values, observable in the $In_{1.6}$ and $In_{1.8}$ spectra, is detected when temperature is lowered.

Impedance Study. Representative impedance data for one composition at two temperatures are shown as impedance complex plane plots in Figure 7; similar plots were obtained for all compositions. At room temperature, a very broad arc is observed in which at least two poorly resolved components can be distinguished. At lowest frequencies, the beginning of a spike is seen

Figure 5. Centerbands of ²³Na MAS NMR spectra for the $Na_{1+x}Zr_{2-x}In_x(PO_4)$ ₃ series at room temperature.

Figure 6. Centerbands of ²³Na MAS NMR spectra for the $Na_{1+x}Zr_{2-x}In_x(PO_4)_3$ series at 200 K.

which is more developed at higher temperatures. The spike has an associated capacitance (calculated from the ideal relation $Z'' = (ωC)^{-1}$), of ~0.1 *μ*F and, since it is inclined to the *^Z*′ axis at [∼]70-80°, it indicates a blocking electrode response; therefore, the conducting species must be ionic, i.e., Na⁺ ions. The total pellet resistance, R_T , is obtained from the intercept of the spike and/or the arc (low-frequency end) on the *Z*′ axis.

Further information on the electrical microstructure of the sample and the separation of possible bulk/grain boundary contributions is obtained from spectroscopic *Z*′′/*M*′′ plots of the same impedance data (Figure 8). At room temperatures, the *M*′′ spectrum shows a broadened peak with associated capacitance (calculated from $M' = C_0/2C_p$ at the maximum) of ∼6 pF. Since the data were not corrected for the capacitance of the sample holder (a few pF, in parallel with the capacitance of the sample), this peak certainly represents the bulk response of the sample; the bulk high-frequency permittivity [calculated from $\epsilon' = CA^{-1}/8.854 \times 10^{-14}$, where *A* is the sample area (area of electrode contact) and *l* the thickness] is in the range $10-50$.

The *M*′′ peak shows a clear shoulder on the lowfrequency side which is approximately coincident with the peak maximum in the *Z*′′ spectrum and has an uncorrected capacitance of \sim 13 pF. This is attributed to a thick grain boundary or constriction resistance at

Figure 7. Impedance complex plane plot for $\text{Na}_2\text{InZr}(\text{PO}_4)_3$ at (a) 297 K and (b) 425 K.

Figure 8. Impedance and modulus spectroscopic plots for Na₂- $InZr(PO₄)₃$ at 297 K.

the region of grain-grain contacts and arises because the pellets were not fully densified. This component dominates the *Z*′′ spectrum and, therefore, forms the major part of the total resistance of the samples. A third component in the overall response is evident as a lower frequency shoulder peak in the *Z*′′ spectrum, with an associated capacitance of ∼50 pF. This is attributed to a more traditional thin grain boundary region and makes a significant contribution to the overall pellet impedance; because its capacitance is quite high, it is

Figure 9. Arrhenius plots of the overall pellets conductivities for the $Na_{1+x}Zr_{2-x}In_x(PO_4)_3$ series.

Figure 10. Arrhenius plots of the frequency maxima of *M*′′ for the $\text{Na}_{1+x}\text{Zr}_{2-x}\text{In}_x(\text{PO}_4)_3$ series.

not readily apparent in the *M*′′ spectrum (*M*′′ peak heights are proportional to C^{-1}).

The overall pellet conductivities, in traditional Arrhenius format, are given in Figure 9. If it is assumed that the capacitances of the different regions are temperature-independent, then the *f*max data reflect the behavior of the corresponding resistances (since the relation $2\pi fRC = 1$ holds, ideally, at the peak maxima). Further, since *R* and *C* for a given component depend inversely on the geometry of the regions concerned, then the *f*max data represent an intrinsic property, independent of geometry or volume fraction. To separate the various contributions to the overall sample impedances, Arrhenius plots of the frequency maxima of *M*′′ peaks are given in Figure 10 and the resulting activation energies in Table 1. The f_{max} data show a gradual increase with *x* for a given temperature, indicating that the bulk conductivity increases with *x*. This trend is not so apparent, however, in the overall conductivity data, since these are significantly influenced by grain boundary impedances.

Discussion

A solid solution with a wide range of compositions, $\text{Na}_{1+x}\text{Zr}_{2-x}\text{In}_x(\text{PO}_4)_3$ (0.0 $\leq x \leq 1.8$), has been synthesized. Observed 31P MAS NMR peaks correspond to the five possible phosphorus environments [P(OZr)4-*ⁿ*(OIn)*ⁿ* $(n=0-4)$]. If a random distribution of Zr and In cations

Figure 11. (010) view (*c*-axis vertical) of two lantern units of the NASICON structure showing the structural variation along the series, as discussed in the text.

in the octahedra occurs, the intensities of the five possible ^{31}P components should be proportional to (2 – *x*)⁴, 4(2 - *x*)³*x*, 6(2 - *x*)²*x*², 4(2 - *x*)*x*³, and *x*⁴ values, which is experimentally confirmed. The intensity ratios of each pair of adjacent bands in each sample, corrected for statistical multiplicities, are near to the $(2 - x)/x$ values. This behavior indicates that the Zr/In distribution is nearly random and rules out the existence of nanoregions with different metal stoichiometries. Sample compositions deduced from the NMR intensities agree with the nominal values. Hence, it can be concluded that the samples have the expected compositions and are chemically homogeneous.

In a previous work, 14 it was shown that the unit cell *a* and *c* parameters of $\text{Na}_{1.4}\text{M}_{1.6}\text{In}_{0.4}(\text{PO}_4)_{3}$ increase in the sequence $Ti < Sn < Hf < Zr$, in agreement with the ionic radii of $\mathrm{M}^{4+,20}$ For the present materials, the unit cell volume expands slightly with substitution of smaller Zr^{4+} by larger In³⁺ and the concomitant increase of Na⁺ content. However, the unit cell changes shape since *a* increases and *c* decreases with *x* (Table 1). These results are in agreement with previous observations.7 The present structural study allows us to explain these changes with *x* at an atomic level.

On the basis of the structural data obtained by the Rietveld refinements, the anisotropic expansion can be rationalized as follows. The decrease in *c* with *x* correlates with a decrease in intralantern $P-O(1)-M$ angles, from 156.9° for In₀ to 150.1° for In_{1.8}, leading to a compression of the lanterns in the *c* direction. Interlantern P-O(2)-M angles do not change appreciably (Table 3). Consequently, the M'''M intralantern distance decreases strongly, although the M'''M interlantern distance (also along the *c*-axis) increases slightly (Figure 11). The evolution of the 31P MAS NMR bands along the series can be rationalized on the basis of these structural changes. The shifts in the 31P peak positions for each set of bands $[P(OZr)_{4-n}(OIn)]$ have been

⁽²⁰⁾ Shannon, R. D. *Acta Crystallogr.* **1976**, *A32*, 751.

correlated with the variation of the $P-O-M$ angles. As the P-O(2)-M angles between adjacent $\rm Zr_2(PO_4)_3$ units (interlantern angles) show negligible variation, the shifts are ascribed to the changes of the intralantern ^P-O(1)-M angles. A similar shift was detected in tectosilicates and assigned to the progressive modification of tetrahedral $T-O-T$ angles of the network with Al/Si substitution.

The filling of the M2 sites produces also a considerable modification of their oxygen environment. For In_0 , the M2 sites are vacant and the void is very anisotropic with four long distances to O(1) (2 \times 3.05 and 2 \times 2.77 Å) and four shorter distances to O(2) (2 \times 2.43 and 2 \times 2.33 Å). As this site is progressively filled, the environment becomes more regular (Table 3): Na(2)-O(1) bond distances become shorter and $Na(2)-O(2)$ distances larger. For In_{1.8}, the distances are 2×2.92 and 2×2.68 Å for O(1) and 2 \times 2.50 and 2 \times 2.48 Å for O(2). The main structural change produced along the series is the movement of O(1) toward the M2 site, which stretches the lanterns, causing the metal to displace from the center of the octahedron toward the O(1) face (Figure 11). This results in an opening of the $O(1)-M-O(1)$ angles and a closing of the $P-O(1)-M$ angles (Table 4). At the same time, a small translation of the $PO₄$ tetrahedra in the *ab* plane, far from the center of the lantern unit (0 0 $\frac{1}{4}$), takes place. The more important degree of freedom, which adjusts along with the incorporation of Na on the M2 site, is the flexibility of the $MO₆$ octahedra, which distort by opening the $O(1)$ face, thus allowing these oxygens to move toward Na(2). The analysis of the structures show that the sizes and shapes of the bottlenecks connecting the M1 and M2 sites (Table 1) do not change significantly along the series.

XRPD refinements are not stable for Na displaced from the M1 site center. However, the room temperature combined NPD and XRPD refinements showed positional disorder at the M1 site and few if any cation vacancies (<2%). The evolution of the thermally induced disorder of Na at M1 sites was analyzed indirectly by T-NPD by checking the *U*iso of Na1 at (000) as a function of temperature. Thermal disorder starts approximately above 250 K for $In_{0.8}$ and above 275 K for $In_{1.6}$ (Figure 3). The temperature dependence of this activation is sharp for $In_{1.6}$ and smoother and larger for the $In_{0.8}$ sample. *U*iso thermal variation of Na at M2, for both samples, is by comparison much smaller. With the limited 2*θ* range of the NPD data and the anomalously very high *U*iso values for Na at M1 above 400 K, it is not possible to confirm full occupancy of M1 at $T \geq 400$ K. So, either more extensive Na(1) spatial disorder or vacancy creation or both may occur at $T \geq 400$ K. The activation of Na at the M1 site has important implications for both 23Na MAS NMR and impedance studies.

The 23Na MAS NMR study gives information about the structural sites occupied by Na and about the changes in Na mobilities as a function of temperature and composition. For $In_{0.2}$ and $In_{0.4}$, two signals are needed to explain the patterns recorded at room temperature. The signal at -13 ppm with $\eta = 0$ (axial symmetry) is assigned to Na at the center of M1 site, but the second signal at -17 ppm with $\eta = 0.8$ must be ascribed to structural sites of lower symmetry. For $x \geq$

0.8, exchange of Na between the structural sites is detected. As a consequence, a unique "envelope" with an intermediate pattern is measured (Figure 5). The averaged signal sharpens with increasing *x*, indicating an increase in sodium mobility. Sodium mobilities were also detected in this series by 23 Na NMR (not MAS) by measuring signal line widths with temperature.¹³

Freezing the samples at 200 K produces a new signal at ca. -8 ppm (Figure 6) that was previously assigned to Na at the M2 site. 14 The intensity of this band increases with *x*, indicating the progressive filling of this site. For $x > 1.2$, NMR components are narrower, indicating the existence of some residual mobility for Na at 200 K. The signal measured at room temperature at -17 ppm does not correspond to any of these signals, and hence, it must be ascribed to a third sodium site. Occupation of these sites must be associated with the thermal spatial disorder detected in the combined NPD and XRPD Rietveld studies. These sites, out of the center of the M1 cavity and near to the structural M1- M2 bottleneck, could minimize the electrostatic repulsion between contiguously occupied M1 and M2 sites. However, for high sodium mobilities, this signal cannot be detected, as rapid Na exchange masks signals of different sites. The low-temperature ²³Na MAS NMR study has confirmed the existence of sodium mobility for all compositions at room temperature and the mobility increases considerably for $x > 0.8$.

The electrical microstructure of the samples is complex, in part due to their incomplete sintering and densification. A thick constriction region between adjacent grains dominates overall conductivities. Nevertheless, the temperature and composition dependence of the bulk response can be obtained readily from the *M*′′ peak maximum and compared with that of the overall pellet. The Arrhenius plots for the overall conductivities in the series do not show a clear trend (Figure 9). However, the *M*′′ data fall on a set of wellspaced approximately parallel lines showing a clear trend of increasing bulk conductivities with *x*. Conductivities increase by almost 2 orders of magnitudes along the series (Figure 10); however, the activation energies are almost constant (Table 1). Therefore, the variation in the *M*′′ *f*max data with *x* must be mainly attributed to variations in carrier concentration. An increase in overall conductivity with *x* has already been reported.7 Hence, when the pellet sintering is not satisfactory, the Arrhenius plot of *M*′′ *f*max gives a good indication of the bulk response of the sample.

Some insights into the similarities and differences between the bulk and thick grain boundary regions are obtained from a comparison of the frequency of the maximun of M' and Z' , f_{max} , versus $1/T$ (Arrhenius plots). Three samples, representative of the behavior of the series, are shown in Figure 12. Due to the frequency limitations of the impedance equipment, M' f_{max} data were obtained over only a limited range of lower temperatures, whereas much more extensive data sets were obtained for *Z'* f_{max} . *M'* f_{max} data occur at $1-2$ orders of magnitude higher than corresponding *Z'* f_{max} data but are essentially parallel for the temperatures over which both *M*′′ and *Z*′′ data were obtained. The parallel behavior of the *M*′′, *Z*′′ plots at lower temperatures shows that the conduction mechanism and the

Figure 12. Arrhenius plots of the frequency maxima of *Z*′′ for ${\rm Na}_{1+x}Zr_{2-x}{\rm In}_{x}({\rm PO}_{4})_{3}$ [$x=0.2$ (\triangle), 0.8 (\heartsuit), 1.6 (\Box)] and of M' for $x = 1.6$ (\blacksquare).

nature of the material is essentially the same in the bulk and thick grain boundary regions of the samples. It is well-established that even in single crystals, the *Z*′′ peaks always occur at lower frequencies than corresponding *M*′′ peaks. In extreme cases, such as Na $β$ -alumina crystals, the peak separation may be 2 orders of magnitude; more commonly peak separations are often about $0.5-1$ order of magnitude. The origin of the peak separations lies in the conduction mechanisms and the fact that the electrical response cannot be represented by simple, ideal, frequency-independent RC elements, but additional, frequency dependent admittances, or constant phase elements, are necessary in order to adequately model the experimental data.

The curvature in the *Z' f*_{max} Arrhenius plots (Figure 12) is of the kind widely seen in materials with high ionic conductivity. At higher temperatures, the *Z*′′ data show curvature toward a region of lower activation energy. The explanation usually given is that, at lower temperatures, some defect clustering or local ordering of the mobile ions occurs, leading to an increase in the activation energy for conduction. The variable-temperature NPD study shows the development of a strong cation spatial disorder at the M1 site over the temperature range where the curvature is observed. Both phenomena are likely related as the relative destabilization of Na at M1 with temperature is probably responsible for decreasing the activation energy. The onset of the new regime slightly depends on the Na content as it occurs at lower temperatures as *x* increases. The existence of two regimes with different sodium mobilities agrees with the NMR results. The Na M1 sublattice "melting" decreases the activation energy as the relative destabilization of that site is essential for ionic conductivity. Charge carriers have to jump through the M1 site in order to migrate.

Conclusions

 $\text{Na}_{1+x}\text{Zr}_{2-x}\text{In}_x(\text{PO}_4)_3\,0.0 \leq x \leq 1.8$ materials are single phase solid solutions and the analysis of the 31P MAS NMR peak intensities showed that homogeneous samples free of segregated nanoregions were synthesized. The structure responds to the incorporation of Na on the M2 site by moving the O(1) atoms toward those sites, reflecting the flexibility of the MO_6 octahedra. Lowtemperature 23Na MAS NMR spectra show low sodium mobilities, allowing the assignment of the two detected signals to Na cations at the M1 and M2 sites. At room temperatures, Na mobility increases with Na content; for $x \leq 0.4$, the Na cations are rather localized, but for $x \geq 0.8$ compositions, important mobility gave a single line with averaged characteristics. The Arrhenius plots for the overall conductivites did not show a systematic trend but the plots of the M' $f_{\rm max}$ data showed a clear increase of bulk conductivities with *x*. T-NPD showed spatial disorder of Na at the M1 site above ∼250 K. The low-temperature activation energies change very little with *x*, in agreement with negligible variation of the bottleneck size. So, the observed increase of conductivity with *x* is due to an increase in charge carrier (Na^+) concentration. The observed curvature in the Z' f_{max} Arrhenius plots, likely related to the strong thermal disorder of Na at the M1 site, indicates the existence of two regimes with different sodium motion (localized at lower temperatures and extended at higher temperatures) in the series.

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